An Answer to Four Papers of Mr. Hobs, lately Published in the Months of August, and this present September, 1671.

In the former part of his first Paper;

Motu) to this purpose (for he doth not repeat it Verbatim:) If there he supposed a row of Quantities infinitely many, increasing according to the natural Order of Numbers, 1,2,3,&c. or their Squares, 1,4,9,&c. or their Cubes, 1,8,27,&c. whereof the last is given. It will be a row of as many, equal to the last, in the first case, as 1 to 2; in the second case, as 1 to 3; in the third, as 1 to 4, &c. (Where all that is affirmed, is but; If we SUPPOSE That; This will Follow. Which Consequence Mr. Hobs doth not deny: and therefore all that he saith to it, is but Cavilling.)

Mr. Hobs moves these Questions, (and proposeth them to the Royal Society, to pass a judgment on them.) 1. Whether there can be understood (he should rather have said, supposed) an infinite row of Quantities, whereof the last can be given. 2. Whether a Finite Quantity can be divided into an Infinite Number of lesser Quantities, or a Finite quantity consist of an Infinite Number of Parts. 3. Whether there be any Quantity greater than Infinite, 4. Whether there be any Finite Magnitude of which there is no Center of Gravity. 5. Whether there be any Number Infinite. 6. Whether the Arithmetick of Infinites

be of any use, for the confirming or confuting any Doctrine.

For answer. In general, I say, 1. Whether those things Be or Be not; yea, whether they Can or Cannot be; the Proposition is not at all concerned, (which affirms nothing either way;) but, whether they can be supposed, or made the supposition, in a conditional Proposition. As when I say, If Mr. Hobs were a Mathematician, he would argue otherwile; I do not affirm that either he is, or ever was, or will be fuch. I only fay (upon supposition) If he were, what he is not; he would not do as he doth. of these Quare's have nothing to do with the Proposition: For it hash not one word concerning Gravity, or Center of Gravity, or Greater than Infinite. 3. That usually in Euclide, and all after him, by Infinite is meant but, More than any assignable Finite, though not Absolutely Infinite, or the greatest possible. 4. Nor do they mean, when Infinites are proposed, that they should Nnn 2 actually

actually Be, or be possible to be performed; but only, that they be supposed. (It being usual with them, upon supposition of things Impossible, to infer useful Truths.) And Euclide (in his second Pollulate) requiring, the producing a streight line Infinitely, either may; did not mean, that it should be actually performed, (for it is not possible for any man to produce a streight line Infinitely; but, that it be supposed. And if AB * be supposed for produced, though but one way; its length must be p. II. supposed to become Infinite (or more than any Finite length affignable;) For, if but Finite, a Finite production would ferve. But, if so produced both ways; it will be yet Greater, that is, Greater than that Infinite, or Greater than was necessary to make it more than any Finite length assignable. (And whoever doth thus suppose Infinites; must consequently suppose, One Infinite greater than a nother.) Again, when (by Euclide's tenth Proposition) the same AB*, may be Bisetted in M. and each of the halves in m, and fo onwards. Infinitely: it is not his meaning (when such continual section is proposed) that it should be adually done, (for, who can do it?) but that it be supposed. And upon such (supposed) lection infinitely continued, the parts must be (supposed) infinitely many; for no Finite number of parts would suffice for Infinite sections. And if further, the same AB so divided, be supposed the fide of a Triangle ABC*; and, from each point of division, supposed lines (as mc, Mc, &c.) parallel 94. IV. to BC: these parallels (reckoning downward from A to BC) must consequently be (supposed) infinitely many; and those, in Arithmetical progression, as 1, 2, 3, &c. each exceeding its Antecedent as much as that exceeds the next before it;) and, whereof the last (BC) is given: (and their Squares, as 1, 4, 9, &c. their Cubes, as 1,8,27,&c.) And this I fay, to shew that the supposition of Infinites (with these attendants) is not so new, or fo Peculiar to Cavallerius or Dr. Wallis, but that Euclide admits it, and all Mathematicians with him; as at least supposable, whether Posible or not.

In particular, therefore, to his Quare's, I answer, I. There may be supposed a row of Quantities Infinitely many, and continually increasing, (as the supposed parallels in the Triangle ABC, reckoning downwards from A to BC,) whereof the last (BC) is given, 2. A Finite Quantity (as AB) may be supposed (by

(by fuch continual Bisections) divisible into a number of parts Infinitely many (or, more than any Finite number assignable:) For there is no stint beyond which such division may not be supposed to be continued; (for still the last, how small soever, will have two halves;) And, all those Parts were in the Undivided whole; (else, where should they be had?) 3. Of supposed Infinites, one may be supposed greater than another: As a, sup. posed, infinite number of Men, may be supposed to have a Greater number of eyes. 4. A surface, or solid, may be supposed so constituted, as to be Infinitely Long, but Finitely Great, (the Breadth continually Decreasing in greater proportion than the Length Increaseth,) and so as to have no Center of Gravity. Such is Toricellio's Solidum Hyperbolicum acutum; and others innumerable, discovered by Dr. Wallis-Monsieur Fermat, and others. But to determine this, requires more of Geometry and Logick than Mr. Hobs is Master of. 5. There may be supposed a number Infinite; that is, greater than any assignable Finite: As the supposed number of parts, arising from a supposed Section Infinitely continued. 6. There is therefore no reason, on this account, why the Doctrin of Euc'ide, Cavallerius, or Dr. Wallis, should be reiected as of no use.

But having folved these Quere's, I have some for Mr. Hobs to answer, which will not so easily be dispatched by him. though Supposed Infinites will serve the Mathematicians well enough: yet, howsoever he please to prevaricate (which, he Lith, is for his Exercise,) Mr. Hobs himself is more concerned than they, to solve such Quære's. Let him ask himself therefore, if he be still of opinion, that there is no Argument in nature to prove, the World had a Beginning: 1. Whether, in case it had not, there must not have passed an Infinite number of years before Mr. Hobs was (For, if but Finite, how many soever, it must have begun so many years before.) 2. Whether now, there have not passed more; that is, more than that infinite number. 3. Whether, in that Infinite (or more than infinite) number of Years, there have not been a Greater number of Days and Hours: and, of which hitherto, the last is given. 4. Whether, if this be an Absurdity, we have not then (contrary to what Mr. Hobs would perswade us) an Argument in nature to prove, the world had a beginning. Nor are we beholden to Mr. Hobs for this Argument; for it was an Argument in use before Mr. Hobs was born. Nor can he serve himfelf felf (as the Mathematicians do) with supposed Infinites; For his Infinites, and more than Infinites of Years, Days, and Hours, already past, must be Real Insinities, and which have actually existed, and whereof the last is given: (and yet there are more to follow.) Mr. Hobs shall do well; (for his Exercise) to solve these, before he propose more Quare's of Insinites. And this I say, to shew that Mr. Hobs is, as much as any, concerned to solve the Quare's by himself proposed.

In the latter part of his first Paper,

E gives us (out of his Roset Prop. 5.) this Attempt of Squaring the Circle, suppose DT be 2DC, and DR a mean proportional between DC and DT: the Semidiameter DC will be equal to the Quadrantal Arc RS, and DR to TV.

That the thing is false, is already shewed in the Latin Confutation of his Rosetum, published in the Philosophical Transactions

for July last past.

As it is now in the English; his Demonstration is peccant in these words, (Col. 2. lin. 31, 32, 33.) Therefore -- the Arc on TV, the Arc on RS, the Arc on CA, cannot be in continual proportion; (with all that follows:) There being no ground for such Consequence.

And the thing is manifest *; for fince that, by his construction, DC.CA. Arc on CA extended: pare in the same cantinual pro-DR. RS. Arc on RS extended: portion, of the Semidiameter DT. TV. Arc on TV extended: to the Quadrantal Arc;

Let that proportion be what you will; suppose, as 1 to 2; and consequently, DC to CA being as 1 to 2. * Sec Tab. I. n. V. it will be to the Arc on CA3 as I to 4: And by the fame reason, DR to the Arc on RS, and DT to the Arc on TV, must also be as 1 to 4: And therefore the Arcs on TV, on RS, on CA; that is, 4 DT, 4 DR, 4 DC; will be in the fame proportion to one another, as (their fingles) DT,DR,DC: But these (by construction) are in continual proportion; therefore those Arcs also, as they ought to be. Indeed, if (by changing some one of the terms) you destroy (contrary to the Hypothesis) the continual proportion of DT, DR, DC, you will destroy that of the Arcs also (which are still proportional to these:) but so long as DT, DR, DG, be in any continual proportion portion (whether that by him assigned or any other) those will be in the same continual proportion with them. As if for DT, DR, DC, be taken Dt, Dr, DC, in any continual proportion (greater, less, or equal to his) the Arcs on tu, on rs, on CA, (extended) will be in the same continual proportion.

But (which is the common fault of Mr. Hobs's Demonstration) if this Demonstration were good, it would serve as well for any proposition as that for which he brings it. For if, instead of \(\frac{2}{5}\), he had said, \(\frac{4}{9}\), \(\frac{1}{100}\), or what else he pleased; the Demonstration had been just as good as now it is, without changing one syllable: That is, it will equally prove the proportion of the Semidiameter to the Quadrantal Arc, to be, what you please: As any may presently see, who doth but read over his Paper.

In his second Paper,

for truth; (and therefore doth no more concern Dr. Wallis, than other men.) And its this, The four sides of a square being divided into any number of equal parts, for example, into 100; and streight lines drawn through the opposite points, which will divide the Squares into 100 lesser Squares: The received opinion (saith he) and which Dr. Wallis commonly useth, is, that the Root of those 100, namely 10, is the side of the whole Square. Which to constute, he tells us, The Root 10 is a number of squares, whereof the whole contains 100; and therefore the Root of 100 Squares is 10 of those squares, and not the side of any Square; because the side of a Square is not a superscies, but a Line.

For An, I say, that its neither the opinion of Doctor Wallis, nor (that I know) of any other (so far is it from being a Receis wed Opinion, which Master Hobs infinuates as such) that 10 is the Root of 100 Squares (For surely a Bare Number cannot be the side of a Square Figure:) Nor yet (as Master Hobs would have it) that 10 Squares is the Root of 100 Squares: But that 10 tengths is the Root of 100 Squares. 'Tis true that the Number 10 is the Root of the Number 100, but not, of a 100 Squares: and, that 10 Squares is the Root (not of 100 Squares, but) of 100 squared Squares: Like as 10 Dousen is the Root, not of 100 Dousen, but of 100 Dousen, but of 100 Dousen, and, as, there,

there, you must multiply not only 10 into 10, but Dousen into DouJen, to have the Square of 10 Dousen; so here to into 10 (which
makes a 100) and Lengthinto Length (which makes a Square) to
obtain the Square of 10 Lengths, which is therefore 100 Squares,
and 10 Lengths the Root of side of it. But, says he, the Root of
100 Soldiers, is 10 Soldiers. Answer. No such matter: For 100
Soldiers is not the product of 10 Soldiers into 10 Soldiers, but of
10 Soldiers into the Number 10; And therefore neither 10, nor 10
Soldiers, the Root of it. So 10 Lengths into the Number 10, makes
no Square, but 100 Lengths; but 10 Lengths into 10 Lengths
makes (not 100 Lengths, but) 100 Squares.

So in all other proportions: As, if the number of Lengths in the Square side be 2; the number of Squares in the Plain will be twice two, (because there will be two rows of two in a row:) If the number of Lengths in the side, be 3; the number of *See Tab. 1. Squares in the Plain, will be 3 times 3, or the Square of 3: If that be 4, this will be 4 times 4: And so in VIII. IX. all other proportions. Of which, if any one doubt

he may believe his own eyes *.

And this Mr. Hobs might have been taught by the next Carpenter (that knows but how to measure a Foot of Board) who could have told him, that because the fide of a Square Foot, is 12 Inches in Length, the Plain of it will be 12 times 12 Inches in Squares: Because there will be 12 Rows of 12 in a Row.

His third Paper,

Which came out just as the Answer to the two former was going to the Press, contains, for substance, the same with his second, and the Latter part of the first: And so needs no farther Answer.

Only I cannot but take notice of his usual trade of contradicting himself. His second Paper says, The side of a Square is not a Superficies, but a Line: His third says the quite contrary, (Prop. 1.) A Square root, (speaking of Quantity) is not a Line, but a Restangle. Other faults, falsities, and contradictions, there are a great many.

As for Instance: He tells us first, In the natural Row of Numbers, 25 1, 2, 3, 4, 5, 6, &c. every one is the Square of some number in the same Row; (that is, of some Integer number;

which is notoriously false.) This he contradicts in the very next words, But Square numbers (beginning at 1) intermit first two numbers, then four then fix, &c ; so that none of the intermitted numbers is a Square number, nor hath any Square root. (If these intermitted numbers, between 1, 4, 9, 16, &c. be not Squares how is it that every one in the whole row is a Square, and that of some Integer number?) But this again is contradicted prop, 2. where 200 (one of such intermitted numbers) is made a square, and 14-4 the Root of it.

Again: in his Definition he tells us, that a Square Root multiplied into it self produceth a Square: But (prop.2.) he multiplieth the Root 14 4 (not into it self, but) into 14 (a part thereof,) to make 200, which he will have to be the Square of that Root. Nor is it a meer slip of negligence in the computation, but his Rule directs to it; Any number given is produced by the greatest Root multiplied into it self, and into the remaining Fraction. Whereof he gives this instance: Let the number given be 200 Squares, the greatest Root is 14-4 Squares (he should rather have said Lengths; but that is a small fault with him;) I say, that 200 is equal to the product of 14 into it self (which is 1963) together with 14 multiplied into 4 (which is equal to 4:) that is 144 multiplied into 14. But this calculation is again contradicted in his third proposition, where he calculates the same square otherwise, as we shall see by and by. In the mean time let's consider this alone, and see the contradictions within it felf. His Rule bids us multiply the greatest Root into it self, &c. This greatest Root he says is 144; yet doth he not multiply this, but 14 (a part thereof) into it self and into the Fraction 4. Again; if 144 be the greatest Root, what shall be the remaining Fraction? Doth he take the Root of 200 to be more than 14 4 by some further remaining Fraction? If so, he should have told us what that Fraction is 3 for 4 it is not this being part of his greatest Root 14 4. But if we should allow (as I think we must,) that by the greatest Root he means sometimes 14-4, sometimes 14, (that is, if we allow him to contradict himself,) yet how comes he by the Fraction $\frac{a}{14}$? For, $\frac{2}{14}$ is too much (the square of $14\frac{2}{14}$ being more then 200, as by multiplying 142 into it felf will appear;) which destroys his whole design; for 14, multiplied into 142, will not make 200, but 198; contrary to his rule. But further, it is so gross a mistake, to make 200 the Square of 1472, that every Apprentice 000

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boy, (that can but multiply whole numbers, and fractions,) could have informed him better, who would first have reduced the fraction to smaller terms, putting $14\frac{2}{7}$ for $14\frac{4}{14}$, and then multiplying $14\frac{2}{7}$ into it felf, would have shew'd him, that the square of $14\frac{4}{14}$, that is, $14\frac{3}{14}$ multiplied into it felf, is (not 200, but) $204\frac{4}{49}$.

But the Root of 200, is the said number 10/2, which is less than 14\frac{2}{14}, and bigger than 14\frac{2}{15}: the Square of that being somewhat more than 200; and, of this, somewhat less; but either of them within an unite of it.

But this fecond Proposition, is (as I said) contra-14 dicted by his third, which makes the Square of 14-4 to be $200\frac{x}{49}$, (by what computation, we shall see by and by;) and then finds fault, that this and the former do not agree. (But 'tis no wonder they should disagree, when both are false.) The same square (saith he) calculated Geometrically, confifteth (by Euclid. 2.4.) of the same numeral great Square 196, and of two Restangles under the greatest side 14 and the Remainder of the side, and further of the Square of the less segment; which altogether make $200\frac{7}{29}$. (He might have learned to reckon better; but let us see how he makes it out.) As by the operation it self (saith he) appeareth thus: The side of the greater fegment is 14-4 (this was, but now, the fide of the whole square, how comes it now to be but the fide of the greater Segment?) which multiplied unto it felf (faith he) makes 200: (103but 204-4:) The product of 14 the greatest Segment into the two Fractions 14 is 4, and that added to 196 makes 200: (if by two fractions 14, he mean, as he ought by his Rule, the Fraction 4 twice taken, or the double of it, it will be not 4, but 8, and this added to 196 make 204; But all this he puts in his pocket, for it comes not into account at all.) Lastly, the product of $\frac{1}{14}$ into $\frac{2}{14}$, or $\frac{1}{7}$ into $\frac{1}{7}$ is which with the first 200 makes 200 1/49: (But he forgets him= felf, for his lesser segment was not $\frac{2}{14}$, but $\frac{4}{14}$; he should therefore have said $\frac{4}{14}$ into $\frac{4}{14}$, or $\frac{2}{7}$ into $\frac{2}{7}$, is $\frac{4}{49}$.) His calculation therefore should have been this: The greater segment is (not $14\frac{2}{14}$) but) 14; which multiplied into it self makes (not 200, but 196. The Rectangle of the greater segment 14, into the lesser 4, is 4: And this taken a second time, is another 4: The lesser seg. ment (not $\frac{2}{14}$, but) $\frac{6}{14}$, or $\frac{2}{7}$, multiplied into it felf, is (not (not $\frac{1}{49}$, but) $\frac{4}{49}$: All which added together make not $200\frac{1}{49}$, but $196 + 4 + 4 + \frac{1}{49} = 204\frac{4}{49}$, which is just the same with $14\frac{1}{49}$ multiplied into it self. So that, had he known how to multiply a number into a number, especially when incumbred with fractions (which it is manifest he doth not,) he would have found no disagreement between the Arithmetical calculation, and what he calls the Geometrical. But I am ashamed (for him) that so great a pretender to such high things in Geometry, should be so miserably ignorant of the common operations of practical Arithmetick.

His repeated Quadrature he now expresseth thus, The Rac dius of a Circle is a mean Proportional between the Arc of a Quadrant and two fifths of the same. But instead of two fifths, he might as well have faid the balf, or tenth, or hundredth part, &c; or (taking T in DC produced beyond C,) the double, decuple, centuple, &c. or what you please: For his Demonstration would have proved it, which is this. Describe a Square ABCD, and in it a Quadrant DCA. In the side DE (continued if need be,) take DI two fifths of DC, (or its Half, Double, Hundredth part, or what you please;) and between DC and DT a mean proportional DR; and describe the Quadrantal Arcs RS, TV. I Jay, the Arc RS is equal to the streight line For seeing the proportion of DC to DT is duplicate of the proportion of DC to DR, it will be also duplicate of the Proportion of the Arc CA to the Arc RS, and likewise duplicate of the Proportion of the Arc RS to the Arc TV. Suppose some other Arc, less or greater than the Arc RS, to be equal to DC, as for example rs; Then the proprrtion of the Arc is to the streight line DT will be duplicate of the proportion of RS to TV, or DR to DT, which is abfurd; because Dr is by construction greater or less than DR. Therefore the Arc RS is equal to the side DC; which was to be demonstrated. Which demonstration therefore proving indifferently every proportion, doth not indeed prove any. In brief: The force of his Demonstration is but this; DT being to DC as 2 to 5 (or in any other proportion) and DR a mean proportional between them; RS will be so between TV and CA; and therefore rs (greater or less than RS,) will not be a mean proportional between TV and CA: which is true; but why it may not be equal to DC, we have nothing but his word for it; there being nothing to shew, that DC is equal to such a mean proportional. Again; though rs be not a mean proportional between TV and CA, yet it may be between to and CA, which serves his Demonstration as well;

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which is indifferent to any three continual proportionals, as was shewed before. So that now we have had three Demonstrations of this Quadrature, (in his Rosetum, in his first paper, and in his third,) and this common fault in all of them, that they equally prove the proportion by him proposed, or any other what you please. But such his Demonstrations use to be.

And this is what I thought fit to fay to Mr. Hobs's Four Papers (rather to satisfie the importunity of others, than because I thought them worth Answering:) And submit the whole, with all Respects, to the Royal Society, to whom Mr. Hobs makes his

Appeal.

His Fourth Paper;

THich came out fince the Three former were answer'd, (containing some faint endeavors to re-affert some

things in them,) is but meer Trifling, or worse than so.

What he would therein infinuate concerning God (that we may as well prove Him to have had a Beginning, as that the World had) imells too rank of Mr. Hobs. We are not to measure Gods Permanent Duration of Eternity, by our successive Duration of Time: Nor, his Intire Vbiquity, by Corporeal Extension.

What in it concerns Mathematicks, (whether his own or others,) is so weak and trivial, (and said only, that he may seem to fay fomething, though nothing to the purple,) that I shall trust it with those to whom he makes his appeal, without thinking it to need any Reply; The view of what he writeth against, being a sufficient Answer to all he saith.

New Observations of Spots in the Sun; made at the Royal Academy of Paris, the 11,12 and 13th of August 1671; and English't out of the French, as follows.

* See Numb-74.p. 2216; whence it will appear, that force such Spors were seen here in Lotidon, A.1660. And Mon . Picard affirm'd to Di. Fogelius at Hamburg, that he had seen sone in October 1661. witness the faid Doctor's own Letter, written to the Fublisher August 11th lift.

T is now about twenty * years fince, that Astronomers have not feen any confiderable spots in the Sun, though before that time, fince the Invention of Telescopes, they have from time to time obferved them. The Sun appeared all that while with an entire brightness, and Signor Caffini saw him so

the ninth of this month of August.

